

## Multibody Dynamics Simulator

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## Chapter 1

## Introduction

Multibody Dynamics Simulator resulted from the PhD work [1 on planar dynamics of rigid bodies with unilateral contacts (as Linear Complementarity Problems-LCP). Most of the theory is covered in the book by Pfeiffer and Glocker [2]. There are many more references, but if you need one book to start, this is it!

Some extensions to the Pfeiffer and Glocker formulations built into the program are:

- arbitrary shape of planar discrete bodies that can have unilateral contacts [3],
- tracking mechanical energy lost at contact surfaces 4,
- geometrical roughness phenomena and run-in wear 4, 5.

The program is written in Delphi 7 and uses GLScene Open GL library for graphics and a modified ParseExpr for handling symbolic mathematical expressions at run-time.
To run the program you need MultiBodyDynamicsSimulator.exe and the qtintfr0.dll; it is recommended that both files are in path.

## Chapter 2

## Running the program

In this section a quick overview on running the program will be given. First a the program in the section 2.1 the Front panel is presented and than in the Section 2.2 the program in shown by a simple example model.
You can skip the Front panel section if you are eager to start using the program ASAP.

### 2.1 Front panel

Figure 2.1 shows the Multibody Dynamics Simulator windows: Main window, Control window, Log window, History window, Jobs window and the Plot window.

### 2.1.1 Control window

Expanded Control window is shown in Figure 2.2 and has this sections:

- World
- LCP Solver. Used to change parameters of the Linear Complementarity Problem Solver (section 3.4.1
- Create next version. Creates next version of the current model. If the current model is in directory 000 , then the new directory will be 001 . Usually, this option is used to create the next version of the model if the model is changing due to wear (section 3.4.2).
- Bodies. Used to change the way the bodies are displayed
- Body. Used to show each body' Bounding Box, Contact Watches (section 3.4.12), get body' mass and mass moment of inertia and also to set transparency (section 3.4.3).
- Collisions. Used to control what happens at collision (section 3.4.1).
- History. Used to control frequency of saved data (section 3.4.1).
- Log. Used to control what goes int the log file/window (section 3.4.1).
- Pointer. Used to set the focus.
- Orientation box. Used to control the orientation box (the room).
- Axes. Used to show the inertial coordinate system.


Figure 2.1: MultiBody Dynamics Simulator.

### 2.1.2 Jobs window

Jobs window is active only if a $J o b$ is running (section 3.4.2). Via this window the execution of jobs can be controlled.

### 2.1.3 History window

Each model has its own folder and each simulation run has a 3digit numerated subfolder (e.g. 000, $001, \ldots$ ). In the history window this subfolders are listed for loading, deleting, resampling. The option Start with this is used to start a new simulation where the selected simulation in the history window ended.

### 2.1.4 Plot window

The Plot window is used to show watches at selected contact points (section 3.4.12).


Figure 2.2: Control window.


Figure 2.3: Plot results window.

### 2.2 Defining a Model-2 Mass Example

The dynamical model is defined by several files (mass matrix, shapes, contact parameters,...). It is advised to create a separate folder for each model.
Each run of a model will create a three digital sub-folder starting with 000 (following with $001,002, \ldots$ ). In this way each simulation can have different parameters or shapes; this is especially useful in wear-in simulations where the body-shapes change with each simulation.

The creation of a simple 2Mass model will shown here.

### 2.2.1 The environment

The main file of a model is the World file.
A simple world file is:

```
[main]
numberOfGeneralizedCoodinates = 3
minimumTimestep = 1e-10
maximumTimestep = 5e-4
maximumPenetration = 1e-5
breakTime = 0.5
[bodies]
body1 = mass1.bdy
body2 = mass2.bdy
```

Detailed specifications for the World file are given in section 3.4.1.

### 2.2.2 Bodies

Each body defined in the World file needs to have a bdy file. A typical body file named mass1.bdy is (section 3.4.3):

```
[main]
name = mass1
RGBcolor = 0 1 0
shapeType = extrusionSolid
shapeFile = mass1.exs
density = 2500
thickness = 0.02
correctOrigin =0
[startPosition]
x = -0.005
y = 0.15
z = 0
Rx = 0
Ry = 0
Rz=3.1459
[startVelocity]
x = 0
y = -1
z = 0
Rx = 0
Ry = 0
Rz=0
```

As defined in the body file (shapeFile $=$ mass1.exs), the shape is defined in mass1.exs shapeFile (section 3.4.4. A simple shape is shown below with listing the $x$ and $y$ points that define the edge of the body.

```
points = 6
%%data
0.07 0.00-0.07 -0.07 0.07 0.07
0.05 0.06 0.05 -0.05 -0.05 0.05
%%enddata
```


### 2.2.3 Generalized coordinates

Generalized coordinates are defined in the $g c$ file (section 3.4.5).
In this simple example we would like the body named mass 1 to have three degrees of freedom ( $x, y$ and $R z)^{1}$
The 2Mass.gc file is:

[^0]```
b'mass1'x[t]
b'mass1'y[t]
b'mass1`Rz[t]
```


### 2.2.4 Dependent coordinates

Generalized coordinates are defined in the $d c$ file (section 3.4.6).
For this simple example the 2Mass.dc file is empty as there are no dependent coordinates. For a nonempty $d c$ file, see section 2.3 .

### 2.2.5 Mass matrix

The mass matrix is defined in the $m m x$ file (section 3.4.10).
The 2 Mass. $m m x$ file is:
b'mass1'm 00
0 b'mass1'm 0
$00 b^{\prime} m a s s 1^{‘} J z z$

### 2.2.6 H Vector

The equations of motion are written in the form $\boldsymbol{M} \ddot{\boldsymbol{q}}=\boldsymbol{H}$ and the $\boldsymbol{H}$ vector is used to describe the dynamics that is not covered by the mass matrix $\boldsymbol{M}$ multiplied by the generalized acceleration vector $\ddot{\boldsymbol{q}}$. The $\boldsymbol{H}$ is defined in the $h v$ file (section 3.4.8).

The 2Mass.hv file is:

```
0
-(c`gravity*b'mass1'm)
0
```


### 2.2.7 Constants

A dynamic model can have several constants that are covered in the cns file (section 3.4.7).
The 2Mass.cns file is:

$$
c^{\prime} \text { gravity }=9.81
$$

### 2.2.8 Mechanical energy

Definition of the mechanical energy is not necessary for running a simulation. However, mechanical energy defined in the file with the me extension (section 3.4.9) is useful for keeping track of the lost energy in the system.

The 2Mass.me file is:
 $\left(b^{\prime}\right.$ mass1'm* $\left(\right.$ Derivative $[1]\left[b^{\prime}\right.$ mass1 $\left.1^{‘} x\right][t]^{\wedge} 2+$ Derivative $\left.\left.[1]\left[b^{‘} \operatorname{mass} 1^{`} y\right][t]^{\wedge} 2\right)\right) / 2$

### 2.2.9 Contact properties

The contact properties are defined in the cop file. To define contact properties between the bodies the names defined in the body file are used and for each body pair (section 3.4.11)

The 2Mass.cop file is:

```
[mass1-mass2]
friction=0.1
restitutionNormal \(=0.7\)
restitutionTangent \(=0.2\)
parameterNi=0
initialTemperature \(=0\)
```


### 2.2.10 Watches

What contact properties should the program keep track off is defined in the Watches file, extension wtc (section 3.4.12).

To keep track of points 0,1 and 2 of the body mass1 in the file looks like this (2Mass.wtc):

$$
\begin{aligned}
& {[\text { mass1] }} \\
& \text { contactWatch }=0-2
\end{aligned}
$$

The watches are written to the file watches.txt, where the header of the watches file is written in the log.txt (section 2.2.12)

### 2.2.11 Running the model

Once the model is defined run the Multibody Dynamics Simulator, go to File/Open and find the folder with the model.wld file. The simulations starts with a click on the green play button. Reduce the Frames Per Second (FPS) in the lower left edge of the Main window, if you want more computer power for calculation and less for visualization. You can rotate the model with the mouse and use short-keys (section 3.3) to zoom in or out. Use the Pointer in the Control window to set focus to an arbitrary point (by default focus is set to the first body of the system).

### 2.2.12 Results

Log file For this example the header looks like this:
time mechanicalEnergy b'mass1'x b'mass1'x' b'mass1'x" b'mass1'y b'mass1'y'...
0
0.49995
time mass1 \#0-impN mass1\#0-impT mass1\#0-work mass1\#1-impN mass1\#1-impT...
***********
[Alert] Break time of 0.50005 s reached.

The first line is the header of the data.txt file.
The 3rd and 4th lines are start and end time, respectively.
The 5 th line is the header of the watches.txt file. Lines from 7 th on are notes about the simulation.

Data file data.txt stores the time series of the simulation.

Watches file watches.txt stores the watches data of the simulation. For each body the accumulated watches data can be shown in the Plot window, Figure 2.3 .

### 2.3 Defining a model - Woodpecker 4 DoF Example

The Woodpecker 3DoF and 4DoF models ware presented and analyzed in detail in the research [3], see Figure 2.4

### 2.3.1 Defining the model with Mathematica packages

For the Multibody Dynamics Simulator a set of Mathematica packages was developed to help with defining the model. The Mathematica notebook for the 2 Mass model is shown in Figure 2.5 And for the Woodpecker 4 DoF model in Figure 2.6. While the Woodpecker model is more complicated than the 2 Mass model, the Mathematica notebook is still simple.


Figure 2.4: Woodpecker 4 DoF model.


Figure 2.5: Mathematica notebook for the 2 Mass system.

```
Libraries
Path to custom libraries
    AppendTo[$Path, "j:/Work Janko/CommonFiles/Math"];
    Needs["MultiBodyDynamics MultiBodyDynamics`"];
WoodpeckerToy - 4 DoF
dr. Janko Slavic,2009
Ir. Janko Slavic,, 2009
Coordinates
Generalized
    Gc:= {
        ac:={
Dependent
DC:={b`bird``[t], b`bird``yt]};
```




```
Kinetic, potential energy and virtual work
Kinetic energy
    Ek[t]|:=
    (*ring*)
```



```
    N(*bird*)
    N
```



```
    VRing[t-]:= \sqrt{}{b}`\mathrm{ ring' ' ' [t] + +b`ring'y'[t] }
Potential energy
    \frac{1}{2}}\mp@subsup{b}{}{\prime}\mathrm{ bird`m*vB
```




2
$\qquad$

Equations of motion
$E M=$ Equationsofmotion $[E k[t]$, Ep $[t]$, GeneralizedForces $[\delta W[t], G C], G C$
Mass matrix and h vector
$\{\mathrm{m}, \mathrm{h}\}=$ MassMatrixAndHector [Ek[t], Ep $[\mathrm{t}]$, GeneralizedForces $[\delta W[\mathrm{t}]$,
Save model for MultiBody Dynamics Simulator
Name of model
filename $=$ "WoodpeckerToy";
filename $=$ "Wood
folder $=" j: / " ;$
Write mass matrix, h vector and mechanical energy
MMXWrite folder <> filename <> ". mmx", m]
HVWrite[folder <> filename <> ". hv", h]
MMXWrite[folder <> filename <> ". mmx", m]
HWWrite[folder <> filename <> ". hv", $h]$
HWWrite[folder <> filename <> ".me", Ek[t] + Ep[t]]
Write generalized and dependent coordinates
GCWrite[folder <> filename <> ". gc", GC]
GCWrite [folder <> filename <> ".dc", Prep
GCWrite[folder <> filename <> ".gc", GC]
GCWrite[folder <> filename <>".dc", PrepareDependentCoordinates [Defi
Define and write constants
C'gravity $=9$.
c. $1 \mathrm{M}=0.01 ;$
$c^{\prime} 16=0.015 ;$

C' gravity = 9.81 ;
c. $1 M=0.01$;
c. $16=0.015 ;$
c' $16=0.015 ;$
c' spring $=0.0056 ;$


Figure 2.6: Mathematica notebook for the Woodpecker 4 DoF system.

With help of the Mathematica packages the Jacobian vector and the Jacobian scalar of the dependent coordinates are automatically generated（section 3．4．6）［2，3］．

The WoodpeckerToy．dc file for the Woodpecker 4 DoF model is shown here：

```
\%\%\%new\%\%\%
b‘bird \({ }^{\text {x }}\) [t]
\%\%definition \(c^{`} 1 \mathrm{G}^{*} \operatorname{Cos}\left[\mathrm{~b}^{‘} \mathrm{bird}^{`} \mathrm{Rz}[\mathrm{t}]\right]+\mathrm{c}^{‘} \mathrm{lM}^{*} \operatorname{Cos}\left[\mathrm{~b}^{6}\right.\) ring \(\left.{ }^{〔} \mathrm{Rz}[\mathrm{t}]\right]+\ldots\)
\%\%J
1
0
-(c'lM* \(\left.{ }^{*} \operatorname{Sin}\left[b^{‘} r i n g{ }^{〔} R z[t]\right]\right)\)
\(-\left(c^{‘} l G^{*} \operatorname{Sin}\left[b^{`}{ }^{6} \operatorname{ird}^{〔} \mathrm{Rz}[t]\right]\right)\)
\%\%j
\(-\left(c^{`} l G^{*} \operatorname{Cos}\left[b^{‘} b \operatorname{bird}{ }^{\wedge} \operatorname{Rz}[t]\right]^{*}\right.\) Derivative \(\left.[1]\left[b^{`} \operatorname{bird}^{`} \mathrm{Rz}\right][\mathrm{t}]^{\wedge} 2\right) \ldots\)
\%\%\%new\%\%\%
b‘bird'y[t]
\%\%definition
```



## 2．3．2 The environment

The WoodpeckerToy．wld file looks like this：

```
[main]
decimalSeparator = .
numberOfGeneralizedCoodinates = 4
minimumTimestep = 1e-12
maximumTimestep = 1e-5
maximumPenetration =1e-6
writeToHistoryMultipleOfMaximumTimestep = 1
breakTime = 1.0
[bodies]
body1 = ring.bdy
body2 = stick.bdy
body3 = bird.bdy
body4 = ringF.bdy
body5 = foot.bdy
body6 = ringSideR.bdy
body7 = ringSideL.bdy
```

From the World file we can see that there are seven bodies in the system（Figure 2．7）．
There is a problem with the ring to stick interaction．The ring is embracing the stick and by using only extrusion bodies this needs to be done by combining four bodies：ring，ringF，ringSide $R$ and ringSideR．

However, to speed-up the computation all the mass properties can be added to one body (e.g. ring) and other bodies can be defined its virtual bodies (see option virtualToBody in section 3.4.3). In this way the ringSide $R$ and ringSideL can have unilateral contact with the stick, while the contact dynamics is actually acting on the body ring.


Figure 2.7: Woodpecker in the Multibody Dynamics Symulator.

### 2.3.3 Defining body shape, contact properties, etc

The Mathematica packages can also help you with creating complex body shapes. Figure 2.8 shows Mathematica notebook for creating the bird shape (exs file).

The contact properties for the system are:
WoodpeckerToy - Bird
dr. Janko Slavic,, 2009
www.fs.uni-I.j.siladisk/_slavid
This file is used to create the exact shape of the bird
Circl[r_, n_]:= Module [{a, i},
Table [{r\operatorname{cos}[2\pi\frac{i}{n}],r\operatorname{sin}[2\pi\frac{i}{n}]},{i,0,n)]
]
Elipse[r1_, r2_, n_] := Module[{a, i},
Table [{r1 此[2\pi\frac{i}{n}],r2\boldsymbol{\operatorname{sin}[2\pi}\frac{i}{n}]},{i,0,n}
]
body Elipse[0.01, 0.02,50];
head = Elipse[0.01,0.01,50];
feet =Elipse[0.015, 0.002, 50];
TranslateData[data, x, y_] := Module[{},
Transpose[{x,y} + Transpose[data]]]

```
```

```
Libraries
```

```
Libraries
Path to custom
Path to custom
    AppendTo[$Path, "j:/Work Janko/CommonFiles/Math"];
    AppendTo[$Path, "j:/Work Janko/CommonFiles/Math"];
    Needs["MultiBodyDynamics`MultiBodyDynamics`"];
    Needs["MultiBodyDynamics`MultiBodyDynamics`"];
```

Path to custom libraries

```
```

Path to custom libraries

```
ata \(=\) Join
ata \(=\) Join
    Take [body, \(\{1,6\}\),
    Take [body, \(\{1,6\}\),
    Take \([\) body, \(\{1,6\}]\),
TranslateData \([\) Take head, \([45,50\}], 0,0.02]\),
TranslateData \([\) Take head, \(\{1,20\}], 0,0.02]\),
    Take \([\) body, \(\{1,6\}]\),
TranslateData \([\) Take head, \([45,50\}], 0,0.02]\),
TranslateData \([\) Take head, \(\{1,20\}], 0,0.02]\),
    TranslateData [Take \([\) head, \(\{1,20)], 0,0.02]\),
TranslateData[Take beak, \(\{17,35\}], 0,0.02]\),
    TranslateData [Take \([\) head, \(\{1,20)], 0,0.02]\),
TranslateData[Take beak, \(\{17,35\}], 0,0.02]\),
    TranslateData [Take[head, \(\{31,32\}], \theta, 0.02]\),
    TranslateData [Take[head, \(\{31,32\}], \theta, 0.02]\),
    ranslateData TTa
    ranslateData TTa
    TranslateData[Take \({ }_{[\text {feet }}\) fed, \(\left.\left.\{20,32\}\right], 0,0\right]\),
    TranslateData[Take \({ }_{[\text {feet }}\) fed, \(\left.\left.\{20,32\}\right], 0,0\right]\),
    TranslateData[Take [feet, \(\{20,32\}], 0,0]\),
    TranslateData[Take [feet, \(\{20,32\}], 0,0]\),
1;
1;
ListPlot [data, Frame \(\rightarrow\) True, Axes \(\rightarrow\) False, PlotJoined \(\rightarrow\) True]
ListPlot [data, Frame \(\rightarrow\) True, Axes \(\rightarrow\) False, PlotJoined \(\rightarrow\) True]


\(a=\operatorname{Min}[\operatorname{Transpose}[\) data \(][[1]]]\)
\(a=\operatorname{Min}[\operatorname{Transpose}[\) data \(][[1]]]\)

Figure 2.8: Mathematica notebook for creation of the Bird shape.
```

[stick-ringSideR]
friction=0.3
restitutionNormal=0
restitutionTangent=0
parameterNi=0
initialTemperature=0
[stick-ringSideL]
friction=0.3
restitutionNormal=0
restitutionTangent=0
parameterNi=0
initialTemperature=0
[stick-bird]
friction=0.3
restitutionNormal=0.5
restitutionTangent=0
parameterNi=0
initialTemperature=0

```

\subsection*{2.4 Defining a model - WearBalls}

WearBalls is a simple model of five balls bouncing and colliding with side-wall and sinusoidally moving ground, Figure 2.9. Here we will discuss how to deal with wear which is defined in the watches file.


Figure 2.9: WearBalls model.

The watches file looks like this:
```

[ball1]
contactWatch = all
directionInside=1
maxChange=0.002
[ball2]
contactWatch = all
directionInside=1
maxChange=0.002
[ball3]
contactWatch = all
directionInside=1
maxChange=0.002
[ball4]
contactWatch = all
directionInside=1
maxChange=0.002
[ball5]
contactWatch = all
directionInside=1
maxChange=0.002

```

The watches file will cause the shape of each ball to change (wear) regarding to the loss of mechanical energy at the surface of the body; where the point with maximum loss of mechanical energy will reshape to the inside for 0.002 m . Running the first version for a few moments create the 000 folder that can be used as a starting model version for job run.

The job file:
```

[main]
jobs $=000-013$
maxMinutesForJob=10
maxMinutesForJobs $=300$
createNextVersionAtEnd=1

```
will start running the (already created) version 000 and at the end it will create the version 001 and start running it. This will continue until the version 013. The shapes of the version 013 are shown in the Figure 2.10


Figure 2.10: WearBalls model after 13 wear cycles.

If the watches file defines the bodyBalancedUpdate wear:
```

[bodyBalancedUpdate]
body $=$ ball1,ball2,ball3,ball4,ball5
maxChange $=0.002$

```
then the wear all bodies is balanced: with maximum wear at the point of maximum loss of mechanical energy of all bodies. The result of version 013 with bodyBalancedUpdate is shown in Figure 2.11


Figure 2.11: WearBalls model after 13 body-balanced wear cycles.

\section*{Chapter 3}

\section*{Specification}

\subsection*{3.1 Units}

All units are \(\mathrm{kg}, \mathrm{m}, \mathrm{s}, \mathrm{rad},{ }^{\circ} \mathrm{C}\).

\subsection*{3.2 Mathematical expression}

The program uses contexts to organize names of symbols.
For example all bodies are in the context \(b\) and each body has its own context that is the same as the name defined in the body file. To access to the coordinate \(x\) of the body named mass1 the mathematical expression is: \(b^{〔}\) mass \(1^{‘} x[t]\).
List of contexts:
b bodies (use bodyName, see also section 3.4.3)
c constants
coordinate possible values: \(x, y, z, R x, R y, R z\)
g denotes generalized coordinate which is not directly bounded to a body
(e) whenever mathematical expression can be used this sign will denote this.

Mathematical expressions are
Mathematical expression can contain:
- Generalized coordinates (see section 3.4.5) and its derivatives (e.g. b'rect'x[t]).
- Mass properties (e.g. b'rect'm, b'rect‘Jzz,...).
- Constants (see section 3.4.7, e.g. c'gravity).
- Mathematical functions like \(\sin (\mathrm{x}), \cos (\mathrm{x}), \operatorname{arcsinh}(\mathrm{x}), \log 10(\mathrm{x}), \ln (\mathrm{x}), \operatorname{logN}(\) base, x\(), \operatorname{sqr}(\mathrm{x}), \ldots\)
- Operands: x!, x^y, *, +, -,...

Note: First derivative (velocity) is denoted by Derivative \([1]\left[b^{\prime} \operatorname{rod}^{‘} \mathrm{x}\right][\mathrm{t}]\) or by \(\mathrm{b}^{\prime} \operatorname{rod}^{〔} \mathrm{x}^{\prime}[\mathrm{t}]\).
Note: \([\mathrm{t}]\) is removed, i.e.: b'rect' \(\mathrm{x}[\mathrm{t}]\) is replaced by b'rect' x . You cannot use functions \(\operatorname{Sin}[\mathrm{t}]\), but you can \(\operatorname{Sin}\left[1^{*} \mathrm{t}\right]\) !

\subsection*{3.3 Shortcut keys}

A zoom in.
shift \(+\mathbf{A}\) zoom-in with adjusting the focus.

Y zoom out.
shift \(+\mathbf{Y}\) zoom out with adjusting the focus.
\(\mathbf{S}\) change font scale (used for contact watches).

B changes background color to white and back.

\subsection*{3.4 File specifications}

\subsection*{3.4.1 World}

\section*{File extension: wld}

Example of a file with default values (used if key is not given):
```

[main]
decimalSeparator $=$.
workingDirectory $=$ current
numberOfGeneralizedCoodinates $=1$
LCPPivotToleranceMin $=1 \mathrm{e}-14$
LCPPivotToleranceMax $=1 \mathrm{e}-10$
LCPLexicoZeroTolerance $=1 \mathrm{e}-8$
$\operatorname{logLCPUnboundedRay}=0$
$\operatorname{logLCPMaxNumberOfIterations~}=0$
ZeroVelocityTolerance $=1 \mathrm{e}-18$
TryToSolveByGoingBack $=0 \quad \leftarrow 1=$ True, $0=$ False
minimumTimestep $=1 \mathrm{e}-12$
maximumTimestep $=1 \mathrm{e}-5$
maximumPenetration $=1 \mathrm{e}-6$
maximumDisplacementFactor $=0.5$
writeToHistoryMultipleOfMaximumTimestep $=1$
writeToHistoryAtCollision $=0 \leftarrow 1=$ True, $0=$ False
writeToHistoryEachTimeStep $=0 \quad \leftarrow 1=$ True, $0=$ False
constantListFile $=$ current.cns
generalizedCoordinatesFile $=$ current.gc
dependentCoordinatesFile $=$ current.gc
massMatrixFile $=$ current. mmx
hVectorFile $=$ current.hv
mechanicalEnergyFile $=$ current.me
contactPropertiesFile $=$ current.cop
watchesFile $=$ current.wtc
breakTime $=1 \quad \leftarrow$ (
[bodies]
body1 $=$ rect.bdy
body2 $=$ circle.bdy

```

LCPPivotToleranceMin, LCPPivotToleranceMax, LCPLexicoZeroTolerance define the parameters for the LCP Solver. In case of problems with obtaining the solution try to change this settings. For more accurate results and for geometrically smaller bodies smaller tolerances should be used.
minimumTimestep and maximumTimestep are the minimum and the maximum allowed time step of the numerical integration, respectively. The maximum time step is in general defined by the numerical integration of the differential equations, while the minimum time step is defined by collisions. The
program automatically adjusts the time step between min and max to achieve the penetration limit maximumPenetration.

TryToSolveByGoingBack if true at unsolvable time-step goes two time-steps back to the history and tries again.
maximumDisplacementFactor maximal displacement is estimated according to the geometry and current velocity and then multiplied by the maximumDisplacementFactor. maximumDisplacementFactor should be between 0.1 (quick) and 10 (slow); smaller values can lead to over-penetrations. The bodydefined maximumDisplacementFactor overrides the world defined (see 3.4.3).
breakTime can be a mathematical expression; however, it is calculated at start only.
\(\operatorname{logLCPUnboundedRay~if~True,~LCP~unbounded~ray~alert~is~written~to~log.~}\)
\(\operatorname{logLCPMaxNumberOfIterations~if~True,~LCP~maximum~number~of~iterations~alert~is~written~to~log.~}\)
ZeroVelocityTolerance Is used to create the set of non-impacting contacts.
Note: current is a special token that can be used to replace for example working directory by the directory of world file.
Token can also be used in the filenames, i.e.: "current.cns" is replaced with "worldFileName.cns".

\subsection*{3.4.2 Job}

File extension: job
Example of a job file with default values (used if key is not given):
```

[main]
worldFile=default.wld
jobs=}\leftarrow\mathrm{ example: 001,005,009
lexicoRandomizationRange=0.0,0.0
createNextVersionAtEnd=0}\leftarrow1=True, 0=Fals
maxLinesInLog=0
maxMinutesForJob=MaxInt
maxMinutesForJobs=MaxInt
framesPerSecond=0
delayStartMinutes=0
exitAtFinish=0}\leftarrow1=True, 0=False

```

Note: the model versions (saved in folders) that are about to be ran need to exist. If there are iterative models that create a new version at the end at least the first version needs to exist.
worldfile if not present then the name of the \(j o b\) file is used.
jobs lists \((000,001,005)\) and ranges can be used (005-015).
lexicoRandomizationRange if set then the LCPLexicoZeroTolerance (see .wld file, section 3.4.1) is randomized at each time-step.
createNextVersionAtEnd if enabled then at the end of job next version is created with blank history files.
command-prompt jobs can be started as parameters in command-prompt.
Example: start \low \hold MultiBodyDynamicsSimulator subdir \(\backslash\) BrushSystem.job
maxLinesInLog can be used to break simulation if the maximum number of allowed log lines is exceeded. If maxLinesInLog=0 the log checking is off.

\subsection*{3.4.3 Body}

File extension: bdy
Example of a file:
```

[main]
name $=$ rect
virtualToBody $=$
RGBColor $=010$
shapeType $=$ extrusionSolid
shapeFile $=$ rect.exs
density $=7900$
thickness $=0.1$
maximumDisplacementFactor $=0.1$
skinThickness $=0.001 \quad \leftarrow$ not needed by default
correctOrigin $=1 \quad \leftarrow 1=$ True, $0=$ False
[Mass properties]
mass $=1$
InertiaXX $=0.004$
InertiaXY $=0.004$
InertiaXZ $=0.004$
InertiaYY $=0.004$
InertiaYZ $=0.004$
InertiaZZ $=0.004$
[startPosition]
$\mathrm{x}=0$
$\mathrm{y}=1.1$
$\mathrm{z}=0$
$\mathrm{Rx}=0$
$R y=0$
$\mathrm{Rz}=0$
[startVelocity]
$\mathrm{x}=0$
$\mathrm{y}=1.1$
$\mathrm{z}=0$
$\mathrm{Rx}=0$
$R y=0$
$\mathrm{Rz}=0$

```

Note: skinThickness defines the maximum depth of body which is checked for penetration (if not set then the default value is: \(100 \times\) maximumPenetration, see 3.4.1.
Note: section Mass properties is optional. If mass and mass moment of inertia ZZ are not defined, then they are calculated by using shape data and density.
Note: if body is virtual to another body use the key virtualToBody to define to which body is virtual to.

Virtual body means that the referenced body uses only the shape of the virtual body to detect collisions. Note: If the extrusion shape file (see 3.4.4) origin is not at the center of mass and the correctOrigin is set to True, then the origin is corrected to start at the center of mass.
maximumDisplacementFactor: the body-defined maximumDisplacementFactor overrides the world defined (see 3.4.1).

\subsection*{3.4.4 ExtrusionShape}

File extension: exs

Example of a file:
```

points = 4
%%data
1.0
1.0
%%enddata

```

Note: extrusion shape needs to be closed (first and last points are the same). It is also important that the inside of the body is on the left hand side in one moves in the direction from first to the last point.

\subsection*{3.4.5 GeneralizedCoordinates}

File extension: gc
Example of a file:
```

b'rect'x[t]
b'rect'y[t]
b'rect'Rz[t]
g'relative1[t]

```

See also section 3.2

\subsection*{3.4.6 DependentCoordinates}

File extension: dc
Example of a file:
```

\%\%\%new\%\%\%
b'bird $^{\text {'x }}[\mathrm{t}] \quad \leftarrow$ coordinate name, see 3.4 .5
\%\%definition
$\mathrm{c}^{\prime} \mathrm{lG}+\mathrm{c}^{\prime} \mathrm{lM} \quad \leftarrow$ position ©
$0 \quad \leftarrow$ velocity (e)
$0 \quad \leftarrow$ acceleration ©
$\% \% \mathrm{~J} \quad \leftarrow$ Jacobian vector
$0 \quad \leftarrow$ according to 1 st generalized coordinate ©
$0 \quad \leftarrow$ according to 2nd generalized coordinate (e)
$0 \quad \leftarrow$ according to 3rd generalized coordinate ©
$\% \% \mathrm{j} \quad \leftarrow$ Jacobian scalar
$c^{\prime} \mathrm{lG}+\mathrm{c}^{\prime} \mathrm{lM} \quad \leftarrow$ ©
\%\%\%new\%\%\%
b‘bird'y[t]
\%\%definition
$\vdots$

```

\subsection*{3.4.7 Constants}

\section*{File extension: cns}

Example of a file:
```

c'force1x = 1
c'force1y = 2
c`gravityz = 9.81

```

Notation: c'constantName
```

c denotes constant object
constantName can be whatever

```

\subsection*{3.4.8 HVector}

File extension: hv
Example of a file:
\[
\begin{array}{lc}
c^{\prime} \text { force } 1 x & \leftarrow(e) \\
c^{\prime} \text { force1y }+c^{\prime} \text { gravityz b'rect'm } & \leftarrow(C) \\
c^{\prime} \text { force1x }\left(c^{\prime} j 1 y \operatorname{Cos}\left[b^{\prime} r e c t^{\prime} R z[t]\right]-c^{\prime} j 1 x \operatorname{Sin}\left[D e r i v a t i v e[1]\left[b^{\prime} \operatorname{rod}^{\prime} x\right][t]\right]\right) & \leftarrow(e \\
+\cdots &
\end{array}
\]

Note: vector length equals the number of generalized coordinates. Mathematical expressions are used ©

\subsection*{3.4.9 MechanicalEnergy}

File extension: me
Example of a file:


Note: mechanical energy should be written in first line.

\subsection*{3.4.10 MassMatrix}

\section*{File extension: mmx}

Example of a file:
\begin{tabular}{|c|c|c|c|}
\hline b'rect'm & 0 & 0 & \(\leftarrow\) (e) \\
\hline 0 & \(\mathrm{b}^{\text {'rect'm }}\) m & 0 & \(\leftarrow\) (e) \\
\hline 0 & 0 & \(\mathrm{b}^{\text {'rect }}\) 'J & © \\
\hline
\end{tabular}

See section 3.2

\subsection*{3.4.11 ContactProperties}

\section*{File extension: cop}

Example of a file:
```

[rect1-rect2] $\quad \%$ there should be names of bodies, see also section 3.4.3
resistingPenetration=T:T
friction $=0.5-1 / \mathrm{vRel}$
restitutionNormal $=0.5-1 / \mathrm{temp}$
restitutionTangent $=0.5$
parameterNi=0
initialTemperature $=0$
[rect1:all]
resistingPenetration=T:T
friction $=0.5$
restitutionNormal $=0.5$
restitutionTangent $=0.5$
parameterNi=0
initialTemperature $=0$

```

Note: contact can be defined between two bodes (e.g. [rect-ball]) or between a body and all other (e.g. [rect:all]). First body:all is read and then overwritten with body-body properties.

Note: contact between two bodies is defined by:
\begin{tabular}{ll} 
resistingPenetration & defines if bodies resist penetration. Possible cases: T:T, T:F, F:T. \\
friction & coefficient of friction function \\
restitutionNormal & coefficient of restitution function in normal direction \\
restitutionTangent & coefficient of restitution function in tangential direction \\
parameterNi & parameter function of tangential restitution function \\
initialTemperature & the initial temperature of a contact
\end{tabular}

Functions of contact can contain any constant values and variables "temp" and "vRel".
\begin{tabular}{ll} 
temp & denotes the contact temperature \\
\(v\) Rel & denotes the absolute value of the relative tangential velocity \\
initialTemperature & the initial temperature of a contact
\end{tabular}

\subsection*{3.4.12 Watches and Reshaping}

File extension: wtc
Example of a file:
```

[common]
timeConstant = 0
reshapingCycles = 1
smoothWorkLeftRight = 0
convertImpulseToForce = 0 \leftarrow1=True, 0=False
cummulativeWork = 0 \leftarrow1=True, 0=False
writeAveragedTDivN = 0 }\leftarrow1=\mathrm{ True, 0=False
absoluteAngleInsteadOfWork =0 \leftarrow1=True, 0=False
[constantsUpdate] % this is body balanced updating (according to the loss of ME)
body = brushpin1,brushpin2,brushpin3
constant = c'brushpin1y,c'brushpin2y,c'brushpin3y
maxChange = 0.2e-6
[changeConstants]
constant = c'springA,c`damping
change = -1,-0.03
[reshapeWindow]
cutHiLowValues = 0.0
standardDeviationRange = -100,+100
[bodyBalancedUpdate]
body = brushpin1,brushpin2,brushpin3
maxChange=0.1e-6
[rect1] % there should be name of the body, see also section 3.4.3
contactWatch=1,2,5-10
[rect2]
contactWatch=5
[rect3]
contactWatch=all
directionX = 0
directionY = 0
directionInside = 0
maxChange =0

```
```

[rect3:0] $\%$ in case of reshapingCycles $=2$ this would be used for even history num-
bers
contactWatch=1-5
directionInside $=1$
maxChange $=1 . \mathrm{e}-6$
[rect3:1] $\%$ in case of reshapingCycles $=2$ this would be used for odd history num-
bers
contactWatch $=6$ - 15
directionInside $=1$
maxChange $=1 . \mathrm{e}-6,-1 . \mathrm{e}-6 \quad \%$ wear, grow combination
[rect4]
contactWatch=all:
[rect5]
contactWatch $=1: 3,[4-5]$

```

Watches. Here are some notes on how to define Watches: the values that will be watched.
contactWatch: define which points of a body should be watched.
contactWatch: use single point (e.g. 1), ranges (e.g. 1-3), combination (e.g. 1,2,3,7-10,15) or all.
contactWatch: use a colon to combine contact points to a single watch (e.g. 1:3 or all:).
contactWatch: if definition inside square brackets (e.g. []) then the impulses are converted from relative normal-tangential coordinate system to the absolute \(x-y\) coordinate system (e.g. [1:3] or [all:]).
timeConstant: if \(>0\) then the output impulse is decayed. This is a simulation of measuring the forces with piezo-electric sensor.
cummulativeWork: if is true then the locally lost work is cummulative (summed).
writeAveragedTDivN: if is true then the watches.txt file includes the running average of the tangential/normal impulse (force).
absoluteAngleInsteadOfWork: instead of work the relative angle of contact point is watched. The output is angle between the normal vector and the absolute x axis (in rad). For consistent output: use only with the option writeToHistoryAtCollision, see section 3.4.1 and use only with not combined point ranges (e.g. \(30-98\) is ok, \(30: 98\) is not).
smoothWorkLeftRight if not zero then, the moving average smoothing is applied to the mechanical energy lost at discrete points that define the body.
bodyBalancedUpdate if set then then the statistical properties (mean, standard deviation,...) are calculated according to all listed bodies (by default the properties are calculated for each body individually). maxChange in the section bodyBalancedUpdate is used instead of the maxChange defined for each particular body. Calculation is effected by the reshapeWindow section.

Reshaping. The selected points that are being watched can also be reshaped, see example in Section 2.4. This is always done in iteratively: e.g. if the current run is numbered 000 and the option createNextVersionAtEnd is enabled (section 3.4.2) then the next version's (001) shape will be reshaped according to the options given below.

Theoretically the approach was presented in 4, (5): The basic idea is that the amount of wear at selected contact points is proportional to the rate of lost mechanical energy. However, at each iteration the maximum change is defined by maxChange occurring at contact point with highest loss of mechanical energy. The direction of reshaping of the contact point is either defined by the body-relative-coordinate: (direction \(X\), direction \(Y\) ) or by the option directionInside. If directionInside is 1 or -1 ( \(1=\) inside, \(-1=\) outside \()\) then the direction \(X\) and direction \(Y\) are calculated for each shape point according to the two neighboring points.
maxChange: defines the maximum reshaping size at the contact point with the highest loss of mechanical energy. maxChange can be as single value or as a range (e.g. maxChange \(=1 \mathrm{e}-6,-1 \mathrm{e}-6\) ). In case of a range the first value is used as maximum change for contact points with mechanical energy below average (left side of Gaussian) and the second value is used as maximum change for contact points on right side of Gaussian. For example: directionInside \(=1\) and maxChange \(=1 \mathrm{e}-6,-1 \mathrm{e}-6\) would cause the points with high loss of mechanical energy (left side of Gaussian) to wear and the points with low or no loss of mechanical energy to grow.
reshapeWindow. Sometimes the loss of mechanical energy is irregular with few points taking over all the mechanical load; consequentially, proportional wear would not be appropriate. The reshape Window options set a filter window for the loss of mechanical energy where cutHiLowValues defines the percentage of data cut at low and at high end (to exclude the irregularities). The option standardDeviationRange defines the range around the mean loss of mechanical energy that is used to calculate the proportional wear.

The reshapeWindow effects: bodyBalancedUpdate, constantsUpdate and all bodies.

Updating constants. There are two ways for changing constants when a next version of a model is created. The first one is called constantsUpdate where the constants are updated according to accumulated mechanical energy of selected bodies. The second one is called changeConstants where the constants are changed for a constant value in the next version. If booth options are enabled, the constantsUpdate is applied first.

In the example above the constants \(c^{\text {'b }}\) bushpin \(1 y, c^{\text {'b }}\) brushpin2y, \(c^{\text {'brushpin3y }}\) will be change proportionally to the total work of bodies brushpin1,brushpin2,brushpin3 for a maximum change \(+0.2 \mathrm{e}-6\). Calculation of the total work is effected by the reshapeWindow section (cutHiLowValues).
changeConstants: a list of constants that are being iteratively updated when creating a new job. the change is constant according to the value set by change. Several constants can be separated by a comma. changeConstants is applied after constantsUpdate.
reshapingCycles In case different reshaping parameters should be used for different versions of the model (each run/version has its own folder, i.e. 001) reshapingCycles can be used. If for example reshapingCycles \(=2\) is used then the section [bodyName:0] is used for even history names (000, 002, \(004, \ldots\) ) and [bodyName:1] for the odd history names ( \(001,003,005, \ldots\) ). Similarly, reshapingCycles=3 would designate versions \(000,003,006, \ldots\)
The program first searches for [bodyName:?] sections and if not successful then for [bodyName] section.

\section*{Bibliography}
[1] J. Slavič. Nonlinear and nonsmooth dynamics of discretely defined system of rigid bodies with unilateral contacts. PhD thesis, Faculty of mechanical engineering, University of Ljubljana, 2005. In Slovene.
[2] F Pfeiffer and Ch Glocker. Multibody Dynamics with Unilateral Contacts. John Wiley \& Sons, Inc, New York, 1996.
[3] J Slavič and M Boltežar. Nonlinearity and non-smoothness in multi body dynamics: application to woodpecker toy. Journal of Mechanical Engineering Science, 220(3):285-296, 2006.
[4] J Slavič and M Boltežar. Simulating multibody dynamics with rough contact surfaces and run-in wear. Nonlinear Dynamics, 45(3-4):353-365, August 2006.
[5] J Slavič, M D. Bryant, and M Boltežar. A new approach to roughness-induced vibrations on a slider. Journal of Sound and Vibration, 306(3-5):732-750, Oct 2007.

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[^0]:    ${ }^{1}$ The program uses contexts to organize names of symbols. All bodies are in the context $b$ and each body has its own context that is the same as the name defined in the body file (bdy).

